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# Investigation of seismic performance on retaining walls

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#### Abstract

For the secure construction of the wall used for retaining purposes in earthquake-prone areas, the seismic effect of both active and passive pressures on the ground must be determined. The impact of waves caused by Rayleigh is not taken into account by pseudo-static and pseudo-dynamic approaches. About 67% of the entire energy from earthquakes is made up of Rayleigh waves. In the present study, the active as well as passive ground pressures are compared using a new pseudo-dynamic approach developed by Deepankar Chaudhary Amey Deepak Katdare. This most recent pseudo-dynamic technique takes into account waves produced by Rayleigh, waves caused by shear, and principal waves. The prerequisite of zero pressure on the earth's surface is accomplished by using this technique.

Keywords: Pseudo dynamic, zero ground stress Rayleigh waves, retaining wall, Mononobe-Okabe method

#### Introduction

The calculation based on the lateral static pressure of the earth on the structure of a retaining wall was made by Coulomb in 1776. When determining the size of the push on the retaining wall, Coulomb employed the equilibrium of forces to obtain the greatest state of passiveness and the least active mode criteria. As a result of the need to investigate a significant number of rupture surfaces in order to pinpoint the crucial failure plane, the challenge is unsolvable. In 1857, Rankine offered a straightforward technique for calculating the highest passive and lowest active ground stress. According to Rankine, the backfill soil experienced shear collapse. The assessment of static pressure on the ground and the construction of the retaining structure are both based on the methods presented by Coulomb and Rankine.

For several decades, masonry construction has been a common structural type used all over the world. In China, buildings made of masonry are still seen as the best choice for rural construction, despite buildings made of reinforced concrete having recently taken over urban development due to their quick construction times. This is because materials for masonry are straightforward and affordable. However, it was found that masonry constructions had poor seismic resilience, and in the earthquake that struck Wenchuan, 74% of all brick masonry buildings fell or suffered significant damage <sup>[1]</sup>. Therefore, it has become a focus of study to enhance the seismic behaviour of masonry constructions in rural areas.

In order to enhance the seismic endurance of buildings made of masonry, several studies, both theoretical and experimental, have been conducted on different components of these structures. On the one hand, investigation into novel structural forms has been done. The impact of the horizontal reinforcement on the earthquake resistance of the specimens was investigated using cyclic tests by Haach et al. <sup>[2]</sup> as shown in figure (1), who developed a novel horizontal trussed reinforcement for concrete-reinforcement walls made from masonry. The findings emphasised that the existence of horizontal reinforcement provides superior fracture control and dispersion. The earthquake resistance of ten single-story buildings constructed with reinforced concrete walls made of masonry was examined by Voon and Ingham<sup>[3]</sup>, along with the impact of imposed axial compressive stresses and shear reinforcement. The outcomes demonstrated that the specimens' shear strength increased the magnitude of the imposed axial stress that was observed. Eldin et al. [4-7], Obaidat et al. [8], Bolhassani et al. [9-11], Ramirez et al. [10-11], and EI-Dakhakhni et al. [12] have all performed studies on the seismic behaviour of concrete with reinforcement walls made from masonry. Additionally, periodic load assessment was done when Ma et al. <sup>[13]</sup> built a shear wall using a unique sort of core-aligned block called a double H-block. According to the findings, the double H-block masonry shear barrier had a high degree of ductility and dissipation of energy. Four unconstrained posttensioned walls of masonry were the subject of an experimental investigation conducted by Hassanili et al. [14, 15].

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(3)

The findings demonstrate that, for a given total starting posttensioned force, the distribution of posttensioned bars affects the specimen's lateral toughness. The unconstrained post-tensioning examples resemble swaying walls, and analogous and pertinent research has also been done by Ryu *et al.* <sup>[16]</sup>, Wight *et al.* <sup>[17]</sup>, Kalliontzis and Schultz <sup>[18]</sup>, and Roseboom and Kowalsky <sup>[19]</sup>.



Fig 1: The masonry bond patterns

#### Mononobe Okabe Method

Mahmoud *et al.* <sup>[20]</sup>, a preliminary approach to calculating the combination of static as well as dynamic pressures of the earth on wall-retaining structures was suggested. This enhanced version of the Coulomb sliding wedge concept, which has its foundation on the plasticity concept, represents the forces of earthquakes by corresponding static force. The technique was created for dry, cohesion-free soil.



Fig 2: The stresses on the soil wedge

The wedge's active force is calculated as:

$$P_{AE} = \frac{1}{2} \gamma H^{2} (1 - k_{V}) K_{AE}$$

$$K_{AE} = \frac{\cos 2(\phi - \theta - \beta)}{\cos \theta \cos 2\beta \cos(\delta + \beta + \theta) [1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \theta - l)}{\cos(\delta + \beta + \theta) \cos(l - \beta)}}]^{2}}$$

$$(2)$$

 $\theta = \tan \left(\frac{kh}{1-kv}\right)$ 

The Mononobe-Okabe active pressure on the earth formula is represented by equation (1).

The passive force  $P_{PE}$  is calculated as:

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$$P_{PE} = \frac{1}{2} \gamma H^2 (1 - k_V) K_{PE}$$

(4)

(5)

$$K_{PE} = \frac{\cos 2(\phi - \theta + \beta)}{\cos \theta \cos 2\beta \cos(\delta - \beta + \theta) [1 - \sqrt{\frac{\sin(\phi + \delta) \sin(\phi + \theta - i)}{\cos(\delta - \beta + \theta) \cos(i - \beta)}}]^2}$$

Where

 $\theta = \tan -1 \left( \frac{kh}{1-kv} \right)$ 

H: Height of wall
i: Slope of backfill
K<sub>AE</sub>: Active earth pressure coefficient
P<sub>AE</sub>: Active force per unit length of wall
P<sub>Pe</sub>: Passive force per unit length of wall
B: Slope of back of the wall with respect to vertical
Δ: Angle of friction between wall and soil
Y: Unit weight of soil
Φ: Soil friction angle

# Pseudo-dynamic method

The examination takes an upward, stiff wall of retention into account. This approach takes into account all varieties of seismic waves, including Rayleigh, shear, and main waves. The material used as the backfill beneath the wall that retains soil is thought to have less cohesiveness. Shear stresses and primary wave velocities (Vs and Vp) under earthquake circumstances are depicted in the figure. The shear modulus of the soil (G), the density of the soil ( $\rho$ ), and the Poisson's ratio of the soil ( $\nu$ ) are all functions of the seismic wave velocities, and the Rayleigh velocity of the wave is a function of KR, where KR is the Rayleigh wave's wave number.

As seen in the image, a thin element with width dx and thickness dz is located at a distance of x from the surface of the wall.



Fig 3: When calculating the active pressure of the earth, an upward retaining structure is taken into account.

Through the assistance of the boundary equilibrium strategy, the forces acting on the wedge are resolved, and the predicted total (static and dynamic) active pressure on the earth is displayed as,

$$P_{ae}(t) = \frac{W \sin(\alpha - \varphi) \pm Q_h \cos(\alpha - \varphi) \pm Q_v \sin(\alpha - \varphi)}{\cos(\delta + \varphi - \alpha)}$$
(6)

The seismic active earth pressure coefficient (Kae) is defined as,

$$\begin{split} K_{ae} &= \frac{2P_{ae}(t)}{\gamma H^2} \end{split}$$

$$K_{ae} &= \frac{1}{\tan \alpha} \frac{\sin (\alpha - \phi)}{\cos (\delta + \phi - \alpha)} \\ &- \left\{ Q_h \left\{ \frac{\gamma k_h}{(-K_R)g \tan \alpha} \frac{\sin \left(\omega t + \frac{K_R H}{\tan \alpha}\right) - \cos \omega t}{\sin (\omega t - K_R x) \left(e^{-qH} + \frac{2qs}{(S^2 + K_R^2)q^2} e^{-SH}\right)} \left[ \frac{2qe^{-qH}}{q^2} - \frac{2qK_R e^{-SH}}{(S^2 + K_R^2)(s)} \right] \right\} \frac{\cos (\alpha - \phi)}{\cos (\delta + \phi - \alpha)} \right\} + \end{split}$$

$$(7)$$

$$\left\{ \frac{(2)k_{V}}{(-K_{R})\tan\alpha} \frac{\cos\left(\omega t + \frac{K_{R}H}{\tan\alpha}\right) - \sin\omega t}{\cos\left(\omega t - K_{R}x\right)} \frac{\left[\frac{2qK_{R}^{2}e^{-qH}}{(s^{2} + K_{R}^{2})q^{2}} - \frac{e^{-qH}}{qK_{R}}\right]}{\left[\frac{2qK_{R}}{(s^{2} + K_{R}^{2})q^{2}} - \frac{qe^{-qH}}{K_{R}}\right]} \frac{\sin\left(\alpha - \varphi\right)}{\cos\left(\delta + \varphi - \alpha\right)}\right\}$$
(8)

By comparing the overall earthquake active resistance that is operating on the wall that is retaining it with regard to the wall's depth, it is possible to determine the amount of seismic active earth's pressure dispersion.

$$p_{ae} = \frac{dp_{ae}(t)}{dz} = \frac{\gamma z}{\tan \alpha} \frac{\sin (\alpha - \varphi)}{\cos (\delta + \varphi - \alpha)} + \left\{ \frac{a_{h}\gamma z}{g(-K_{R})\tan \alpha} \frac{\cos(\omega t + \frac{K_{R}z}{\tan \alpha}) - \cos \omega t}{\sin(\omega t - K_{R}x) \left(e^{-qz} + \frac{2qs}{(S^{2} + K_{R}^{2})q^{2}}e^{-sz}\right)(q)} \frac{\cos (\alpha - \varphi)}{\cos (\delta + \varphi - \alpha)} \right\} - \left\{ \frac{a_{v}\gamma z}{g(-K_{R})\tan \alpha} \frac{\sin \left(\omega t + \frac{K_{R}H}{\tan \alpha}\right) - \cos \omega t}{\sin (\omega t - K_{R}x)} \frac{\left[\frac{2qK_{R}^{2}e^{-qz}}{(S^{2} + K_{R}^{2})q^{2}} - \frac{e^{-qz}}{K_{R}}\right]}{\left[\frac{2qK_{R}}{(S^{2} + K_{R}^{2})q^{2}} - \frac{e^{-qz}}{K_{R}}\right]} \frac{\sin (\alpha - \varphi)}{\cos (\delta + \varphi - \alpha)} \right\}$$
(9)

#### **Condition of Passive Resistance**



Fig 4: Calculating the active pressure of the earth, an upward wall of retaining is taken into account.

Assume a fixed-base vertically cantilever structure AB with a height H that supports a horizontal backfill with minimal cohesiveness, as shown in Fig. a piece that is dz in thickness at z distances from the highest point of the wall that is retaining and dx in width at x distances.

Overall passive resistance (static and dynamic) is calculated by applying the limit state of equilibrium technique to the forces acting against the wedge.

$$P_{pe}(t) = \frac{W \sin(\alpha + \phi) \pm Q_h \cos(\alpha + \phi) \pm Q_v \sin(\alpha + \phi)}{\cos(\alpha + \delta + \phi)}$$
(10)

The seismic passive earth pressure coefficient (K<sub>pe</sub>) is given as

$$K_{pe} = \frac{2p_{pe}(t)}{\gamma H^2}$$
(11)

$$K_{pe} = \frac{1}{\tan\alpha} \frac{\sin(\alpha+\phi)}{\cos(\alpha+\delta+\phi)} - \left\{ \frac{2a_{h}}{g\gamma H^{2}(-K_{R})\tan\alpha} \frac{\cos[\omega t - K_{R}(\frac{H}{\tan\alpha})]}{\sin(\omega t - K_{R}(x))\left[e^{-qz} + \frac{2qs}{[s^{2}+K_{R}^{2}]q^{2}}e^{-sz}\right]} \left[\frac{2qe^{-qH}}{q^{2}} - \frac{2qK_{R}e^{-sH}}{[s^{2}+K_{R}^{2}](s)}\right] \frac{\cos(\alpha+\phi)}{\cos(\alpha+\delta+\phi)} \right\} + \frac{2a_{v}}{g(-K_{R})\gamma H^{2}(K_{R})\tan\alpha} \frac{\sin[\omega t - K_{R}(\frac{H}{\tan\alpha})]}{\cos(\omega t - K_{R}(x))} \frac{\left[\frac{2q(K_{R})e^{-sz}}{[s^{2}+K_{R}^{2}](-s)} - \frac{q}{q}\right]}{\left[\frac{2qK_{R}}{[s^{2}+K_{R}^{2}]q^{2}} - \frac{e^{-qz}}{K_{R}}\right]} \frac{\sin(\alpha+\phi)}{\cos(\alpha+\delta+\phi)}$$

$$(12)$$

The distribution of the seismic passive earth pressure  $\left(p_{pe}\right)$  is given by

$$p_{pe}(t) = \frac{dp_{pe}(t)}{dz} = \frac{\gamma z}{\tan \alpha} \frac{\sin(\alpha - \phi)}{\cos(\alpha + \delta + \phi)} + \left\{ \frac{a_{h}\gamma z}{g(-K_{R})\tan \alpha} \frac{\cos[\omega t - K_{R}(x)]}{\sin(\omega t - K_{R}(x))(e^{-qz} + Be^{-sz})(qz)} \frac{\cos(\alpha - \phi)}{\cos(\alpha + \delta + \phi)} \left[ \frac{2qe^{-qH}}{q^{2}} - \frac{2qK_{R}e^{-sH}}{[s^{2} + K_{R}^{2}](s)} \right] \right\} - \frac{a_{v}\gamma z}{g(-K_{R})\tan \alpha} \frac{\sin[\omega t - K_{R}(x)]}{\cos(\omega t - K_{R}(x))} \frac{\left[ \frac{2q(K_{R})e^{-sz}}{[s^{2} + K_{R}^{2}](s)} - \frac{e^{-qz}}{q} \right]}{\left[ \frac{2qK_{R}}{[s^{2} + K_{R}^{2}]q^{2}} - \frac{e^{-qz}}{K_{R}} \right]} \frac{\sin(\alpha - \phi)}{\cos(\alpha + \delta - \phi)}$$
(13)

Where,

- Acceleration due to gravity; g
- Ĥ Height of retaining wall;
- Seismic passive earth pressure coefficient; Kpe
- Wave number for Rayleigh wave; K<sub>R</sub>
- k Seismic acceleration coefficient;
- $k_h, k_v$ Seismic acceleration coefficient in horizontal and vertical directions, respectively;
- Dynamic passive resistance; Ppe

$$\mathbf{q} = \sqrt{K_R^2 - \left(\frac{\omega^2}{V_p^2}\right)}$$

$$s = \sqrt{K_R^2 - \left(\frac{\omega^2}{V_s^2}\right)}$$

- Т Period of lateral shaking;
- t Time;
- Vp Primary wave velocity;
- $V_R$ Rayleigh wave velocity;
- Shear wave velocity;  $V_s$
- Angle of inclination of failure surface to the horizontal; α
- Unit weight of soil; γ δ
- Wall friction angle;
- ø Soil friction angle; and
- Angular frequency of base shaking. ω

#### **Results and Discussions**

Shear wave velocity,  $V_s = 80$  m/s, ratio of primary and shear wave velocity,  $V_p/V_s = 1.87$  and ratio of Rayleigh and primary wave velocity,  $V_R/V_p = \alpha K_{Rs}$ ,

Where

$$\alpha = \sqrt{(1-2\nu)/(2-2\nu)}$$
 and  $K_{Rs}^6 - 8K_{Rs}^4 + (24-16\alpha^2) K_{Rs}^2 + 16(\alpha^2 - 1) = 0$  with  $K_{Rs} = \frac{V_R}{V_c}$ ;

Unit weight of soil:  $\gamma$  16 KN/m<sup>3</sup>; Height of wall: H: 5 m; Poisson's ratio of soil: v 0.3

# $K_{pe}$ variation with the failure plane ( $\alpha$ )



Fig 5: KPE variation with  $\alpha$ 

The point of failure plane is defined as 20. The valve for Kpe decreases as the failure plane angle increases, reaching its lowest at 20 before beginning to increase once more.

# Soil Friction Angle's Effect on Ppe



Fig 6: Variation of PPE

The passive pressure of the earth throughout the height of the structure rises as the soil angle of friction rises from  $32^{\circ}$  to  $40^{\circ}$ , and it is discovered to be at its highest for a soil friction angle of  $40^{\circ}$ . As the soil angle of friction rises from 36 to 40 degrees at a height ratio of z/H = 1, passive pressure increases by roughly 8.14%.

# Effect of $K_h$ and $K_v$ on the $K_{pe}$



Fig 7: Effect of Kv and Kh on KPE

The Kpe valve improves with a rise in the earthquake horizontal coefficient valve, while Kpe decreases with a rise in the earthquake vertical coefficient valve.

### Effect of the Rayleigh wave velocity on K<sub>pe</sub>



Fig 8: Effect of the Rayleigh wave on Kpe

The Kpe valve decreases as the Rayleigh velocity of the wave rises, reaching a maximum at 40 m/s.

# Effect of failure plane on Kae

Soil friction angle ( $\alpha$ ): 32° t/T: 0.03



Fig 9: Effect of failure plane on Kae

The Kae valve grows along with the failure plane angle and achieves its maximum at 34.9. The Kae valve then closes less.

# Effect of soil friction angle on the seismic active pressure $P_{ae} \label{eq:pressure}$

The flow through the distribution valve for seismically active pressure decreases as the soil internal friction angle increases. If the soil angle of friction is increased from 32 to 40 at z/H = 1, there is a drop of 4.20% in the  $P_{ae}/\gamma H$  valve.

# Effect of Rayleigh wave velocity on K<sub>ae</sub>



Fig 10: Effect of Rayleigh wave on Kae

The valve of Kae decreases and approaches a minimum speed of 50 m/s as the Rayleigh wave velocity rises. The Kae valve is then enlarged as the velocity rises.

# Comparison of Seismic passive pressure by Mononobe–Okabe and Deepankar Chaudhury (new method)

Soil friction angle:  $32^{\circ}$ Wall friction angle:  $\phi/2$ K<sub>v</sub>: 0.2 K<sub>v</sub>: 0.5 K<sub>h</sub> t/T: 0.40



Fig 11: Dynamic passive pressure distribution



Fig 12: Passive pressure by M0 method

When the elevation of the wall used for retaining is compared to the earthquake passive pressure using the new technique and the Mononobe-Okabe method, it is discovered that the pressure has increased by 10.56%.

#### Comparison of seismic active pressure by MO and Deepankar Chaudhury (New method)

Soil friction angle:  $32^{\circ}$ Wall friction angle:  $\phi/2$  $K_h$ : 0.2  $K_v$ : 0.5  $K_h$ t/T: 0.40  $K_{ae}$ : 0.449



Fig 13: Active pressure by M0 method



Fig 14: Dynamic Seismic active pressure

The earthquake's active pressure rises as the retaining wall's height increases. The pressure has increased by 7.97% when compared to the new method and the MO method.

### Comparison of Kaeby Both Methods

Soil friction angle:  $32^{\circ}$ Wall friction angle:  $\phi/2$ K<sub>h</sub>: 0, 0.1, 0.2, 0.3



Fig 15: Comparison of Kae by both Methods

In all methods, the valve for Kae also grows when the valve for Kh increases. In comparison to the MO approach, the Kae valve has decreased by 61.18% using the new way.

#### **Comparison of K**<sub>pe</sub> by Both Methods

Soil friction angle:  $36^{\circ}$ Wall friction angle:  $\phi/2$ K<sub>h</sub>: 0, 0.1, 0.2, 0.3



Fig 16: Comparison of Kae by both Methods

In all approaches, Kpe drops as the valve of Kh rises. The KPE valve has decreased by 49.24% in the new approach compared to the MO method.

#### Conclusions

Deepankar Chaudhury's (new pseudo-dynamic) technique takes into account all waves, including those generated by Rayleigh and principal waves. The Mononobe-Okabe approach is employed for the pseudo-static analysis. There is a rise of 7.97% when comparing earthquake active pressure using the new method with the Mononobe-Okabe approach. There is an increase of 10.56% when comparing the new approach to the MO method for passive pressure. When comparing the two methods, the Kae valve has a drop of 61.18%. The KPE disparity is 49.24%. The addition of the Rayleigh wave effect accounts for the differences between different valves. Therefore, it is essential to consider Rayleigh waves when analysing retaining walls.

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